

## Dependence of Association in Polyacrylonitrile Solutions on the Molecular Volume of the Nonsolvent

R. B. BEEVERS, *University of Bradford, Bradford, 7, England*

### Synopsis

An examination of data obtained from viscometric measurements of the association occurring in solutions of polyacrylonitrile in dimethylformamide,  $\gamma$ -butyrolactone, and dimethylacetamide has shown that the solubility parameter of the solvent-nonsolvent liquid mixture at the aggregation point is closely related to the molecular volume of the nonsolvent used to bring about association.

The kinetic features of the association occurring in solutions of polyacrylonitrile in *N,N'*-dimethylformamide (DMF) have been examined in some detail.<sup>1</sup> Viscometric measurements made over a range of temperatures<sup>2</sup> and with a variety of nonsolvents<sup>3</sup> have established that association occurs through dipolar interaction between CN groups along the polymer molecule. It has been shown<sup>1</sup> that large changes occur in the viscosity number of the solution over a narrow range of nonsolvent composition. It has been found convenient to characterize the association by determining the vol-% nonsolvent  $P$  at which the association rate constant has a value of  $1 \times 10^{-6} \text{ sec}^{-1}$ .

Although qualitatively the association of the various solvent-nonsolvent systems so far examined is similar, the primary effect of the nonsolvent is to determine the volume concentration at which association occurs. It has been shown<sup>3</sup> that a relationship exists between the solubility parameter  $\delta_{\text{NS}}$  of the nonsolvent and  $P$  as follows:

$$100/P = A\delta_{\text{NS}} - B \quad (1)$$

where  $A$  and  $B$  are constants. Calculations carried out subsequently as a result of an examination of the effect of variation of the solvent on the association in polyacrylonitrile solutions has shown that the solubility parameter of the liquid mixture  $\delta_a$  at a composition corresponding to  $P$  showed much less variation than the values of  $\delta_{\text{NS}}$ . Initially it was considered that  $\delta_a$  had a constant value for a particular solvent or nonsolvent system, but since association can be observed in systems for which  $\delta_{\text{S}} \geq \delta_{\text{NS}}$ , then clearly this supposition was unrealistic. Subscripts S and NS are here taken to denote the solvent and nonsolvent components, respectively. A misplaced parameter led to calculations being made of the molecular volumes of the nonsolvents used, and it was found that variation in  $\delta_a$ , although subjected

to a significant error, was closely related to changes in molecular volume of the nonsolvent. This was an observation of some interest and gave a basis for remarks previously made<sup>1</sup> that the nonsolvent acted principally as a diluent.

If the volumes of solvent and nonsolvent required to cause association with a rate constant of  $10^{-6} \text{ sec}^{-1}$  are  $v_s$  and  $v_{NS}$ , then

$$P = 100v_{NS}/(v_s + v_{NS}) \quad (2)$$

and it can be shown that the corresponding wt-% nonsolvent  $w_{NS}$  and mole fraction  $x_{NS}$  are given by

$$w_{NS} = 100/(1 + \alpha P') \quad (3)$$

$$x_{NS} = 1/(1 + \alpha \beta P') \quad (4)$$

For convenience, the ratio of the densities  $\rho_s/\rho_{NS} = \alpha$ , the ratio of the molecular weights  $M_{NS}/M_s = \beta$ , and  $P' = 100/P - 1$ . Since  $x_s + x_{NS} = 1$ , it follows that

$$x_s/x_{NS} = \alpha \beta P'. \quad (5)$$

If it is assumed that the solubility parameter for the liquid mixture is given<sup>4</sup> by

$$\delta_a = (x_{NS}V_{NS}\delta_{NS} + x_sV_s\delta_s)/(x_{NS}V_{NS} + x_sV_s) \quad (6)$$

where  $V_s$  and  $V_{NS}$  are the molecular volumes of the two liquids then substitution from eq. (5); and since

$$V_{NS}/V_s = \alpha \beta, \quad (7)$$

it follows that eq. (6) may be written as

$$\delta_a = (\delta_{NS} + P'\delta_s)/(1 + P') \quad (8)$$

or

$$P' = (\delta_{NS} - \delta_a)/(\delta_a - \delta_s). \quad (9)$$

Since  $\delta_a$  will always lie between  $\delta_{NS}$  and  $\delta_s$ , then  $P'$  will always be positive. Calculation of  $\delta_s$  for DMF has been made using boiling point data<sup>3</sup> to give  $\delta_s = 11.60 \pm 0.03 \text{ (cal/cm}^3\text{)}^{1/2}$ , and this now permits  $\delta_a$  to be calculated from eq. (9) as shown in Table I. It is clear that  $\delta_a$  is not constant. Corresponding values of the molecular volumes calculated at 25°C using the density values given by Timmermans<sup>5</sup> are given in the last column and show that  $\delta_a$  gradually decreases with increase in  $V_{NS}$ . With the exception of results for acetone and benzyl alcohol, a very close correlation exists between the two parameters, as follows:

$$\delta_a = C - DV_{NS} \quad (10)$$

the constants  $C$  and  $D$  having values  $12.4 \pm 0.1$  and  $0.014 \pm 0.004$ , respectively, for results obtained in DMF.

TABLE I  
Calculated Values of Molecular Volumes of the Nonsolvents Used  
and of Solubility Parameters for the Solvent-Nonsolvent Mixtures  
Causing Association in Polyacrylonitrile Solutions at 25°C

Nonsolvent	$\delta_{NS}$ , (cal/cm <sup>3</sup> ) <sup>1/2</sup>	$P$ , %	$\delta_a$ , (cal/cm <sup>3</sup> ) <sup>1/2</sup>	$V_{NS}$ , cm <sup>3</sup> /mole
N,N'-Dimethylformamide <sup>a</sup>				
Water	21.2	7.1	12.2	18.1
Methanol	12.9	16.5	11.7	40.7
Ethylene glycol	14.7	13.1	11.9	55.9
Acetone	9.3	45.8	10.5	74.0
<i>n</i> -Propanol	10.3	14.7	11.3	75.1
Isopropanol	9.81	16.0	11.2	76.9
Benzene	9.05	31.1	10.7	89.4
<i>n</i> -Butanol	9.77	16.8	11.2	92.0
Carbon tetrachloride	8.64	21.1	10.9	96.5
Benzyl alcohol	10.9	19.4	11.4	103.8
Toluene	8.92	28.7	10.8	106.9
$\gamma$ -Butyrolactone				
Benzene	9.05	18.1	12.1	89.4
Carbon tetrachloride	8.64	15.9	12.1	96.5
N,N'-Dimethylacetamide				
Benzene	9.05	23.9	10.3	89.4
Carbon tetrachloride	8.64	18.3	10.4	96.5

<sup>a</sup> Values of  $\delta_{NS}$  and  $P$  are taken from Beevers.<sup>3</sup>

Values of  $\delta_a$  have also been calculated for solutions of polyacrylonitrile in N,N'-dimethylacetamide and  $\gamma$ -butyrolactone, using benzene and carbon tetrachloride as nonsolvents. Calculated values of  $\delta_s$  for the two solvents are  $10.73 \pm 0.03$  (cal/cm<sup>3</sup>)<sup>1/2</sup> and  $12.72 \pm 0.03$  (cal/cm<sup>3</sup>)<sup>1/2</sup>, respectively, and lie on either side of the value for DMF. Plotting the results to show the dependence of  $\delta_a - \delta_s$  on  $V_{NS}$ , as in Figure 1, shows that the solvent has little effect on the association in these solutions.

Substituting for  $\delta_a$  in eq. (8) gives eq. (1) with

$$\begin{aligned} A &= 1/(C - DV_{NS} - \delta_s) \\ B &= \delta_s/(C - DV_{NS} - \delta_s) \end{aligned} \quad (11)$$

so that

$$B/A = \delta_s. \quad (12)$$

Substitution of values previously found<sup>3</sup> for  $A$  and  $B$ , namely  $0.80 \pm 0.07$  and  $3.3 \pm 1.5$ , respectively, gives about half the value cited above for  $\delta_s$ . However the inclusion of  $V_{NS}$  in the denominator of eq. (10) must vitiate the use of an equation of the form of eq. (1) to describe the association in polyacrylonitrile solutions. It is clearly preferable, as shown in Figure 1, to calculate  $\delta_a$  from the experimentally determined value of  $P$  and relate

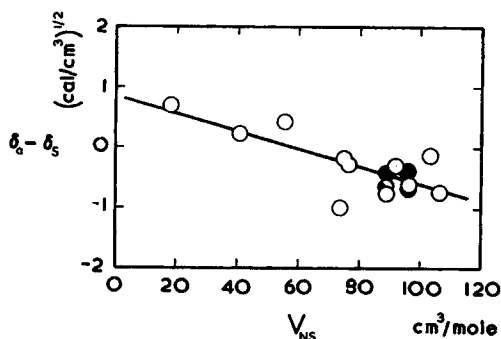


Fig. 1. Dependence of  $\delta_a - \delta_s$  on the molecular volume of the nonsolvent  $V_{NS}$  for association in polyacrylonitrile solutions at 25°C: (O) dimethylformamide; (●) dimethylacetamide; (◐)  $\gamma$ -butyrolactone.

this to the molar volume of the nonsolvent used. More careful examination of the results in Table I confirms this view. Previously the scatter of points about the line represented by eq. (1) had been considered to be indicative of the experimental error, especially in view of the diverse nature of the nonsolvents used. Since  $\delta_a$  will depend on the choice of nonsolvent, it is necessary to compare nonsolvents which have similar values for  $\delta_{NS}$ . Carbon tetrachloride and toluene are similar in this respect; yet a relatively large difference exists between their values of  $P$  and which is not in accordance with eq. (1). The data for the two nonsolvents, however, fit correctly when plotted according to eq. (10). Association data for the isomers  $n$ -propanol and isopropanol also fit correctly with the dependence of  $\delta_a$  on molar volume.

For solvent-nonsolvent systems in which  $|\delta_s - \delta_{NS}|$  is comparable, the amount of nonsolvent required to cause association will decrease with decrease in the molecular volume of the nonsolvent. The specific chemical nature of the nonsolvent is not in evidence in Figure 1, so that, as previously, the nonsolvent may be considered to act by blocking the interactions which occur between the polymer and solvent. Molecular size is not necessarily directly involved at the site of an interaction; but clearly when considering the nonequilibrium statistics of the distribution of nonsolvent molecules, molecular size will become of importance through its effect on molecular mobility.

### References

1. R. B. Beevers, *Polymer*, **8**, 419 (1967).
2. R. B. Beevers, *Polymer*, **8**, 463 (1967).
3. R. B. Beevers, *Polymer*, **9**, 535 (1968).
4. H. Burrell, *Interchem. Rev.*, **14**, 331 (1955).
5. J. Timmermans, *Physico-Chemical Constants of Pure Organic Compounds*, Elsevier, New York, 1950.

Received September 9, 1969